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Characterising Hydrogen Bonds Cooperativity, Electron Density Topology

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The 'simple' Pauling definition

- partially electrostatic
- resonance hybrid
- partially covalent (Isaacs et al. (1999))
- interaction of the type -X...H-Y-, where both X and Y are electronegative atoms
- geometry dependent

Not suitable for rigid formalisation

"... Like most chemical concepts, this term [hydrogen bonding] is more or less universally understood by the practitioners in the field but is not precisely defined

.... This topic is one for interesting debates at tea or coffee times in chemistry departments around the world but is not suitable for rigid formalisation... "

An Unknown Referee (2004)

The more rigorous theoretical definition too confining

"...We have previously taken the position that the intramolecular hydrogen bonding between adjacent ring OH are definably hydrogen bonds, having strong interaction energy and showing synergistic effects in cellobiose..."

"...There is some evidence suggesting that these interactions should not be called hydrogen bonds because they do not demonstrate a bond critical point (BCP) of correct (3,-1) topology. Although this definition is theoretically very critical we will continue to use the term hydrogen bonding for these terms since most scientists in the field of carbohydrate chemistry will find the more rigorous theoretical definition too confining..."

Anonymous Author (2004)

Roald Hoffmann suggests that a chemical bond lies beyond the domain of physics and is incapable of precise physical understanding

"...And yet the concept of a chemical bond, so essential to chemistry, and with a venerable history, has a life, generating controversy and incredible interest. Even if we can't reduce it to physics Push the concept to its limits, accept that a bond will be a bond by some criteria, maybe not by others, respect chemical tradition, have fun with the richness of something that cannot be defined clearly, and spare us the hype..."; Whether physics does or does not offer a definition of a *chemical bond*, it does set out the necessary and sufficient conditions for two atoms to be *chemically bonded* to one another, conditions summarised by Slater in terms of the two theorems that are essential to the physics of bonding: *"... both the virial theorem and Feynman's theorem are exact consequences of wave mechanics. Both interpretations agree in pointing to the existence of overlap charge density as the essential feature in the attraction between the atoms...*";

this article makes a modest proposal: reserve the name and concept of a *bond* for use by those who believe that chemistry lies beyond the scope of physics (in spite of their reliance on molecular orbitals and valence bond structures), and reserve the concept of *bonding* for use by those intent on the pursuit and understanding of chemistry using the tools of quantum mechanics;

Cortes-Guzman & Bader (2004) quoting Roald Hoffmann at the ACS Symposium on "Contemporary Aspects of Chemical Bonding" in September 2003

The Controversy

- Should an interaction such as O...H-O be called a 'Hydrogen Bond'?
- The German '*Wasserstoffbrücke*' means a 'hydrogen bridge'- perhaps more accurate and inclusive as more descriptive
- if we wish to maintain the term 'Hydrogen Bond' we need to define precisely what is meant by a 'bond' in quantum mechanical terms

The Controversy

- How far can we rely on *small* experimental spectroscopic shifts?
- DFT and electron density topology
- Computed and experimentally determined electron density topologies show remarkable agreement
- are classic van der Waals atomic radii (Pauling or Bondi) appropriate?

Answers?

- Is COOPERATIVITY diagnostic of hydrogen bonding as opposed to other types of relatively weak interactions (dispersive, dipole-dipole or van der Waals interactions)?
- Should we define hydrogen bonding in terms of electron density topology?

Benchmarking

• Three lemmas:

- **EXIST** Intermolecular or intramolecular hydrogen bonds that satisfy geometrical criteria and have a (3,-1) bond critical point (BCP)
	- Water clusters and clathrate cages also enols, o-hydroxybenzoic acids, nucleic acids, peptide $α$ -helices and $β$ -pleated sheets, etc.
- **ASSUMED** -Intramolecular hydrogen bonds with marginal geometry and no (3,-1) BCP although with minimal NMR and IR shifts
	- diols and sugars, specifically glucopyranose.
- CANNOT EXIST Hydrogen bonds in which the hydrogen atom cannot interact with the oxygen lone pairs on geometrical grounds but which do have (3,-1) BCPs

– Methane 5^{12} eicosamer and $6^{2}5^{12}$ tetracosamer clathrates.

Data Generation

Water Clusters and Clathrate Cages

Ice Polymorphs

Ih

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sI Clathrates (512 and 51262 cages)

 0°

Cooperativity in Rings

2-coordinated rings *R.A. Klein, IUPAC Pisa September 2005*

2-coordinated rings *R.A. Klein, IUPAC Pisa September 2005*

Fused 2-ring Systems ([2n-1]mer)

Cooperativity in rings

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Cooperativity in Ring Systems

Fig. 4. Raman spectra of the new ice phase compared with ices I, II, III, V, VI, and water measured in situ in the diamond cell. Ice I is proton disordered; ice II is proton ordered; ice III is partially proton disordered but has a proton-ordered form (ice IX); ice V is partially proton disordered. We suggest that ice VI is partially ordered as well. The spectrum of supercooled water is in good agreement with previous work [for example (27)]. Weak peaks <100 cm⁻¹ in that spectrum arise from spurious scattering. The tick marks denote characteristic Raman peaks discussed in the text: bands at 192, 490, 3215, and 3410 cm⁻¹ for the new phase; 145 and 157 cm⁻¹ for ice VI; and 95 and 190 cm⁻¹ for ice III. Intensity is given in arbitrary units. Detailed analysis of the spectra of the additional phases will be presented elsewhere.

from Chou et al.; *Science* (1998) 281, 809

Figure 2. Raman spectra of lattice vibrations and $O-H$ vibrations around $100-400$ and $3000-4000$ cm⁻¹, respectively, of sI hydrate. The asterisks denote characteristic Raman peaks for weak C-H vibration of methane molecules in the cages of the sI hydrate discussed in the text. For comparison, the intensity for hydrate samples is reduced in a same scale, even though it is given in arbitrary units. The experimental conditions for replacement are 278 K and 3 MPa (CO₂).

from Yoon et al.; *J. Phys. Chem. A* (2004) 108,5057

Experimental data (red) from Chou et al. (1998) *Science* 281, 809

Raman-active Vibrations

• Water -11°C

- 3177 ± 68 cm⁻¹ (24%)
- 3378 ± 155 cm⁻¹ (65%)

• Ice Ih -15°C

- 3080 ± 24 ; 3107 ± 116 cm⁻¹ (66%)
- 3277 \pm 200; 3347 \pm 73 cm⁻¹ (34%)

• Ice II -40°C

- 3182 ± 31 ; 3119 ± 62 cm⁻¹ (47%)
- 3300 ± 27 ; 3307 ± 125 cm⁻¹ (53%)

• sI Methane Hydrate

- $3058 \pm 10 \text{ cm}^{-1}$ (7%)
- 3146 ± 105 ; 3153 ± 29 cm⁻¹ (55%)
- 3357 ± 103 cm⁻¹ (38%)

**all peaks obtained by fitting experimental data

Calculated Raman Vibrations

- • Rings 3-7
	- cooperative in-phase $3090-3400$ cm⁻¹
	- cooperative in- and out-of-phase 3240-3460 cm⁻¹

•Undecamer/Heptadecamer/Tricosamer

- cooperative in-phase $3075-3087$ cm⁻¹
- cooperative in- and out-of-phase 3107-3121 cm⁻¹
- cooperative in- and out-of-phase 3100-3320 cm⁻¹ (broad multiple)

•Eicosamer/Tetracosamer

- cooperative annular and polar 3143-3168 cm⁻¹
- cooperative in- and out-of-phase 3220-3300 cm⁻¹

**MPW1PW91/6-311+G(2d,p)

IR and Raman Spectroscopy

- pentamer and hexamer ring
- undecamer
- heptadecamer
- \bullet tricosamer
- •tetracosamer

-O...H-O- Cooperativity

- vibrational relaxation 740 \pm 25 femtoseconds;
- for resonant intermolecular energy transfer (RIET), interaction between H₂O molecules must be extremely strong;
- concentration dependence for rotational anisotropy decay shows that RIET occurs for the OH excitation:
- for dipole-dipole Förster-type interaction, rate of energy transfer, $k = T_1^{-1} * [r_0/r]^6$, where is the lifetime of the T_1 is the excited state and r_0 the Förster radius;
- •experimental T₁ = 4.0 \pm 0.4 ps; r₀ = 2.10 \pm 0.05 Å comparable to O...O in liquid water implying that RIET will be very fast;
- also higher orders and anharmonic coupling;
- Woutersen, S.; Bakker, H.J.; (1999) *Nature* 402, 507

Diols and Glucopyranose

[1,n]-Diols

Scheme 1. Three-dimensional, minimised structures for the (α, ω) diols discussed in detail in this article, namely: ethane-1,2-diol (12EG); propane-1,3-diol (13PG); butane-1,4-diol (14BD); pentane-1,5-diol (15PD); and hexane-1,6-diol (16HD).

[1,n]-Diols - Geometry

Topological analysis of the bond critical points (BCP), with topology (3,-1), for the intra-molecular hydrogen-bond O-H...O in diols excluding 1,2-diols and butane-2,3-diol. Geometries were obtained using MPW1PW91/6-311+G(2d,p); (d) is the electron density at the BCP in a.u.; 2 (d) its Laplacian in a.u.; BCPs were located 34-35% of the bond length from the H atom; ellipticities were in the range 0.02 - 0.09.

Bond critical points (BCPs)

Figure 4. Electron density plot for butane-1,4-diol. Details are as given in the legend to Figure 3.

Table 9. Integrated Atomic Properties for the O-H Atoms in Representative $(n, n + m)$ -Diols, for $n = 1, 2$ and $m = 1-5$.

Diol	H Atom	$E(\Omega)$	$q(\Omega)$	$\mu(\Omega)$	$Vol(\Omega)$	BCP
12EG(B)	$O-HD$	-0.3872	0.5665	0.1567	21.2113	No
	O_A -H	-0.3940	0.5577	0.1628	22.8329	
12PG(A)	$O-HD$	-0.3854	0.5688	0.1553	20.6514	No
	O_A -H	-0.3961	0.5550	0.1623	22.9274	
12PG (B)	O - H_D	0.3855	0.5690	0.1557	20.7952	No
	O_A -H	-0.3956	0.5523	0.1652	23.1882	
13PG	$O-Hp$	-0.3765	0.5866	0.1391	16.8615	Yes
	O_A -H	-0.3921	0.5589	0.1624	22.7929	
12BD	$O-HD$	-0.3864	0.5675	0.1565	21.0780	No
	O_A -H	-0.3932	0.5525	0.1628	21.9069	
13BD (A)	$O-HD$	-0.3764	0.5871	0.1365	16.2861	Yes
	O_A -H	0.3926	0.5596	0.1621	22.8109	
13BD (B)	$O-HD$	-0.3771	0.5837	0.1411	16.9087	Yes
	O_A -H	-0.3942	0.5505	0.1693	23.7924	
$m23BD$ (B)	$O - HD$	-0.3859	0.5677	0.1558	20.7362	No
	O_A -H	-0.3961	0.5509	0.1670	23.3739	
2M13PG (A)	$O-HD$	-0.3778	0.5845	0.1396	16.8912	Yes
	O_A -H	-0.3929	0.5593	0.1621	22.7031	
2M13PG (B)	$O-H0$	-0.3762	0.5879	0.1375	16.4937	Yes
	O_A -H	-0.3926	0.5595	0.1623	22.7305	
14BD	$O - H_D$	-0.3732	0.5917	0.1290	14.3823	Yes
	O_A -H	-0.3914	0.5606	0.1616	22.6916	
12PD	$O - H_D$	-0.3891	0.5637	0.1567	21.2651	No
	O_A -H	-0.3948	0.5530	0.1630	21.9432	
15PD	$O-HD$	-0.3724	0.5938	0.1290	14.4315	Yes
	O_A -H	-0.3915	0.5616	0.1610	22.5602	
m _{24PD}	$O-HD$	-0.3744	0.5901	0.1360	16.0912	Yes
	O_A -H	-0.3964	0.5515	0.1651	23.2529	
12HD	$O-HD$	-0.3883	0.5648	0.1564	21.1668	No
	O_A -H	-0.3938	0.5545	0.1625	21.7989	
16HD	$O-HD$	-0.3752	0.5853	0.1340	14.8101	Yes
	O_A -H	-0.3927	0.5593	0.1617	22.6310	
m25HD	$O-HD$	-0.3745	0.5888	0.1303	14.4607	Yes
	O_A -H	-0.3931	0.5555	0.1653	23.1626	

The abbreviation O-H_D refers to the donor H atom; O_A-H to the acceptor O atom; $E(\Omega)$, the total energy; $q(\Omega)$, the atomic charge; $\mu(\Omega)$, the dipolar polarization; and Vol(Ω), the atomic volume. All values are given in atomic units. BCP indicates whether a bond critical point of $(3, -1)$ topology was detected for the hydrogen bond.

Figure 7. The relationship between the number of carbon atoms in (α, β) ω)-diols ($n = 2-6$) against the change in occupancy of the OH $σ^*$ antibonding orbital (\triangle) , the stabilization energy calculated by secondorder perturbation analysis (\Diamond) or Fock-matrix element deletion (\blacklozenge) , and the percentage s-character for the interacting LP electrons (\triangle) , for the $-$ O $-$ H_D... O_A $-$ interaction determined as described in the text.

Glucose.6H₂O

IR red-shifts and NMR downfield shifts are continuous

red-shift (cm-1)

Figure 1B. Average difference (the 'red-shift') between the IR hydroxyl stretching frequencies for the -O_x-H and -O- H_D bonds in each of diols studied plotted against the -O_s. H_D interaction distance, based on the data shown in Figure 1A. The filled diamonds (*) represent average data for 1,2-, 1,3-, 1,4-, 1,5- and 1,6diols (the last two are single points); the open circle (O) indicates the average value for 1:1 complexes between the different conformers of ethane-1,2-diol, propane-1,2-diol and butane-2,3-diol, with water2.

from Klein, R.A.; (2003) J. Comp. Chem. 24, 1120

Figure 5.

Average difference in DFT-GIAO calculated ¹H chemical shifts for the O-H₀ and O_x-H hydroxyl group hydrogen atoms in 1,2-, 1,3-, 1,4-, 1,5- and 1,6-diols (\blacklozenge), and in cooperative 1:1 water-(n, n+1)-diol complexes (O).

Glucose and Hydrated Glucose

Table YY . OH stretching frequencies in cm⁻¹ (relative intensity) for glucose hexahydrate. Assignments are shown for the various cooperative modes involving sugar hydroxyl groups and the bidentate hydrogen bonded water molecules.

Table XX. O-H_D bond lengths in Ångstrom and cooperativity for ethanediol and glucose in the absence and presence of water of hydration.

4C1-glucose shows *negative* **synergism between OH groups**

Natural bond orbital (NBO) analysis³³ of a series of 1,n-diols ($n = 2-6$) with the two hydroxyls in the same conformation with respect to one another as in the tGg' conformer of ethane-1,2-diol, gives an average electron occupancy for the σ^* anti-bonding orbital of the non-interacting O-H groups of 0.00550 \pm 0.00033. Electron occupancies for the interacting OH σ^* anti-bonding orbital rise from a value of 0.00921 for ethane-1,2-diol to a maximum of 0.02926 for butane-1,4diol, decreasing to 0.02187 and 0.02045 for pentane-1,5- and hexane-1,6-diol, as reported previously^{bb}. By contrast, in glucose-⁴C₁ the σ^* occupancies for the putatively hygrogen-bonded ring OH groups range from 0.00652 to 0.00908 with a mean value of 0.00755 \pm 0.00085; these are significantly less than for ethane-1,2-diol, the reference structure, and are again in the *opposite* direction to that predicted on the basis of any possible cooperative hydrogen bonding. On the other hand, in hydrated ethane-1,2-diol or glucopyranose, where cooperative hydrogen bonding is possible, OH σ^* anti-bonding orbital occupancies range from 0.02655 (diol OH) and 0.02109 (water OH) in the 1:1 ethane-1,2-diol/H₂O complex, to an average value as high as 0.04548 \pm 0.01000 for the O-H bonds in glucose and 0.03695 \pm 0.00541 for those of its associated waters underlining the degree of cooperativity attained. Cross-ring hydrogen bonding in ${}^{1}C_{4}$ -glucose, involving OH1...O6, OH3...O1, and OH2...O4, gives rise to OH σ^* anti-bonding orbital occupancies of 0.02115, 0.02270 and 0.01708, respectively.

4C1-glucose does not form intra-molecular hydrogen bonds

Thus based on all the criteria referred to above, 4C_1 -glucopyranose does not form intramolecular hydrogen bonds between the neighbouring or vicinal ring OH groups. This is not merely theoretical 'hair-splitting' as without evidence for hydrogen bond formation there are no grounds for invoking non-existent synergistic or cooperative effects, especially when conformational equilibria in aqueous solution are being considered, conditions under which the sugar ring will be completely hydrated and where donor-acceptor cooperativity is possible with the formation of a network of inter-molecular hydrogen bonds.

Methane Clathrates

Eicosamer 5¹²

CH4...O Interactions

Tetracosamer 4x4

Methane Electron Density Topology Electrostatic Moments

Clathrate Vibrational Frequencies

Methane-Clathrate 13C-NMR Chemical Shielding Tensors

Suitable and Sufficient?

• Hydrogen bonds

- must satisfy certain geometrical criteria, i.e., donoracceptor distances, -X:...H-Y- angle, H points towards a lone-pair
- show elongation of the H-Y- bond associated with IR red-shifts and NMR downfield shifts (n.b.: bond shortening and blue-shifts)
- demonstrate a (3,-1) bond critical point (BCP) both experimentally and theoretically
- show charge-transfer between donor and acceptor
- show changes in anti-bonding orbital occupancies

Suitable and Sufficient?

- Hydrogen bonds
	- and be characterised by **cooperativity** defined in terms of synergism resulting in greater than simple additivity of effects, i.e., bond length, electron density topology, and spectroscopic parameters.

References

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Thank You

for your attention