

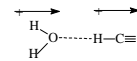
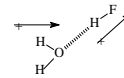
## The Importance of Cooperative Interactions In Hydrogen-Bonding Interactions

## What are Hydrogen Bonds?

### Hydrogen Bonds -What Are they?

Are they due to:  
 Electrostatic Interactions?  
 Polarization?  
 Covalent Interactions?

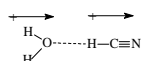
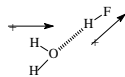
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Water and HCN form a H-bonding dimer that is consistent with a dipole-dipole electrostatic interaction

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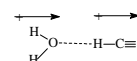
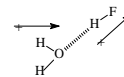
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Electrostatic interactions cannot explain all H-bonding

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Three (or more) centered?

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Materials:  
Crystals  
Aggregates  
Proteins

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### Computer experiments

Can do experiments with computer that  
would be impossible in laboratory.

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Peptides are like solid as the H-bonds have fixed orientations

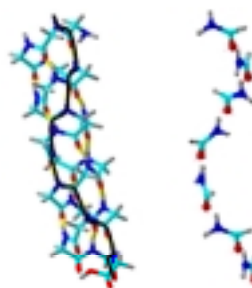
## Cooperativity in H-Bonded Systems Modeling Elements of the Secondary Structure of Proteins

Hydrogen bonds are among the strongest interactions of non-covalent nature. They play an important role determining conformations and binding in many biological systems. An understanding of the quantitative aspects of the hydrogen bonding may lead to the building of more precise models for the processes of biological importance.

In this study we present data that reveals a high degree of cooperativity for hydrogen bonding

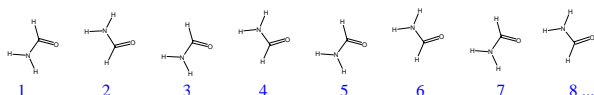
- in formamide aggregates that mimic the H-bonding in helices and antiparallel  $\beta$ -sheets
- in the various  $3_{10}$ - and  $\alpha$ -helical structures
- In models of  $\beta$ -sheets

## H-bonding chains in the



One of the three H-bonding chains in an  $\alpha$ -helix. The H-bonding chains turn in the opposite direction to the covalent bonds in the polypeptide because there are 3 H-bonding chains

## H-Bonding Formamide Chains



•The repeating unit is **two** formamides

•We shall define the numbering scheme from the left:  
the terminal  $\text{NH}_2$  is formamide number 1

Kobko, N.; Paraskevas, L.; del Rio, E.; Dannenberg, J. J. *J. Am. Chem. Soc.* **2001**, *123*, 4348  
Kobko, N.; Dannenberg, J. J. *J. Phys. Chem. A* **2003**, *107*, 10389.

## Methods

Geometric optimization of all the formamide aggregates was conducted at the B3LYP/D95\*\* level using GAUSSIAN98 suite. Full CP-optimizations were performed for the flat chains of up to five formamides.

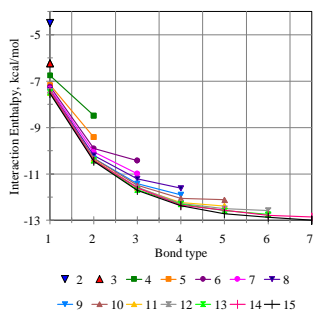
The H-bond interaction energy for each H-bond within an aggregate of N formamides was calculated according to the following equation:

$$E_{\text{mer}} = E_N - (E_m + E_{(n-m)}) + ZPVE + BSSE$$

where m and (n-m) are the sizes of the two smaller aggregates that remain after the H-bond is broken; ZPVE and BSSE are the corrections for one H-bond.

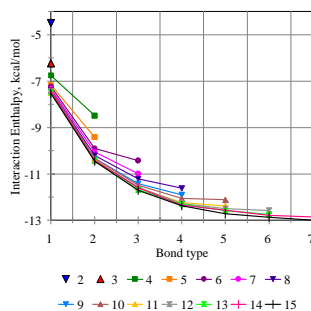
Kobko, N.; Dannenberg, J. J. *J. Phys. Chem. A* **2003**, *107*, 10389

### H-bonding enthalpies for flat formamide chains



Kobko, N.; Dannenberg, J. J. *J. Phys. Chem. A* 2003, 107, 10389

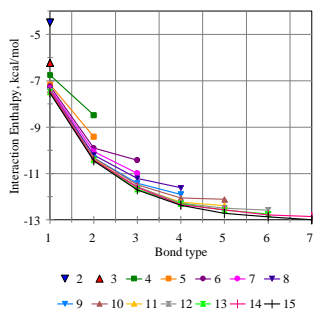
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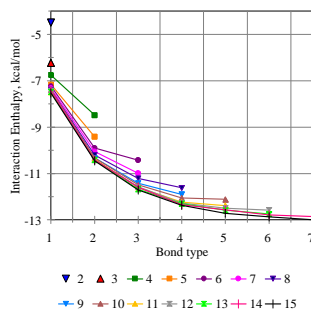


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The middle H-bonds of the 15-mer is roughly 3.0 times as strong as the H-bond of the dimer

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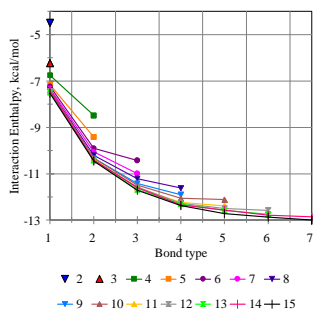
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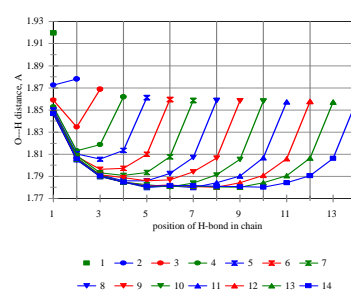
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Cooperativity is not primarily electrostatic

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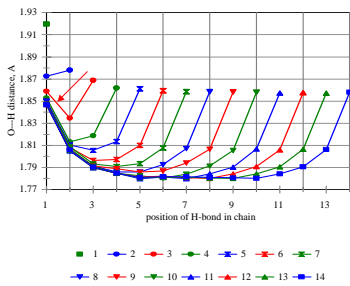
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The length of the hydrogen bond decreases as the chain becomes longer (the middle H-bond of the 15-mer is shorter than the H-bond in dimer by about 0.14Å)

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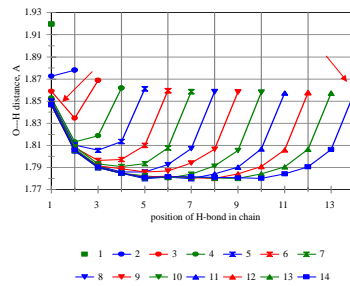


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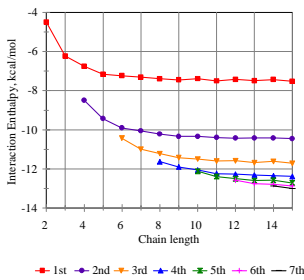


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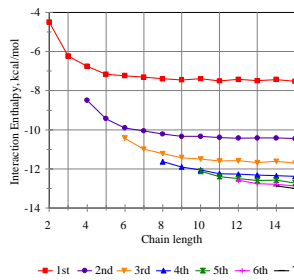
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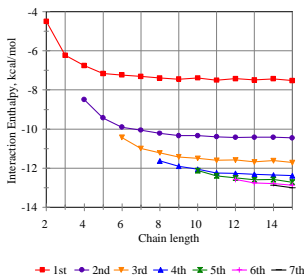
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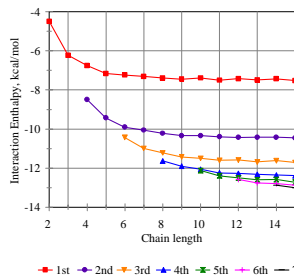


The energies of each type of H-bond reach individual asymptotic limits

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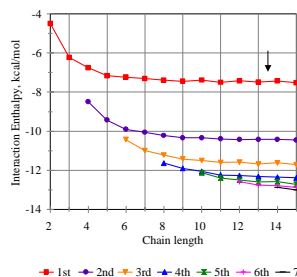
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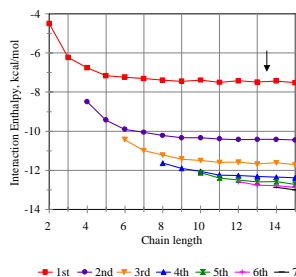


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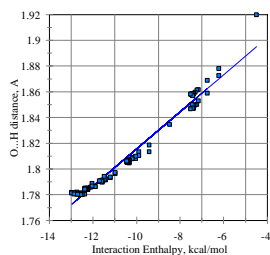
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They are most obvious when the H-bond energy is close to its limiting value

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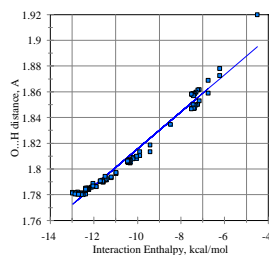
### H-bonding distances vs. interaction energies of the terminal and middle hydrogen bonds in flat formamide chains



H-bonding distances vary with the calculated H-bond energies in a regular quasi-linear manner.

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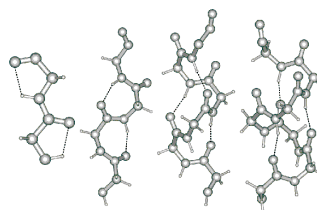
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We should also note that there can be two non-equivalent H-bonds that have the same enthalpy but different length.

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## Helical Peptides

### Conformers of glycine polypeptide



1. repeating unit of the C5 conformer (flat);
  2. two repeating units of the C7 conformer;
  3. two repeating units of the  $3_{10}$  helix conformer;
  4. one repeating unit of the  $\alpha$ -helix (or  $4_{13}$  helix) conformer (seven residues).
- Hydrogen bonds are shown by dotted lines.

Fig.2 Ref.12b Schematic drawing of the conformers of glycine



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- System is divided into up to three levels (high, medium and low). We use only two.

Morokuma and Frisch

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- ONIOM energy is equal to the entire system calculated at low level with the polyglycine calculated at the high level substituted for the low-level

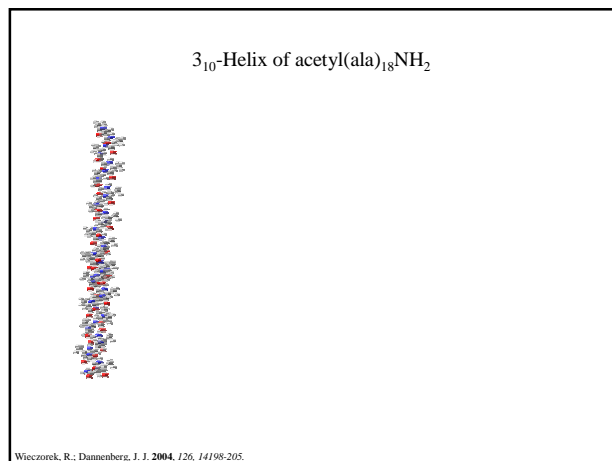
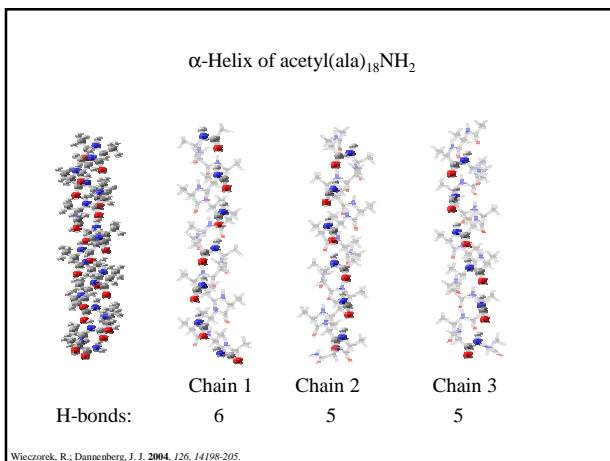
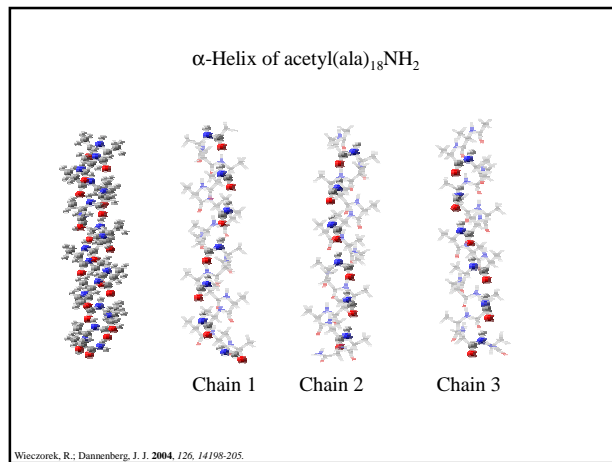
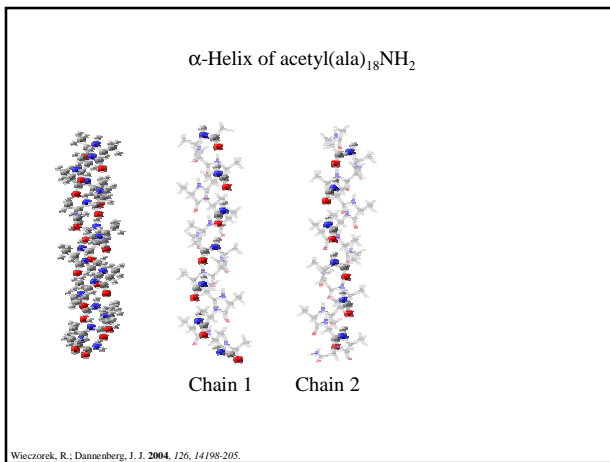
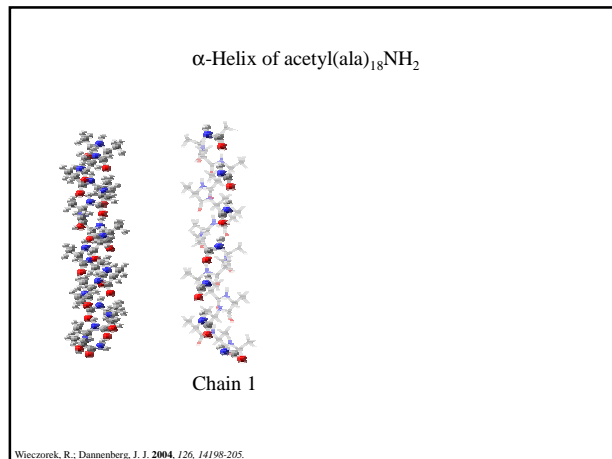
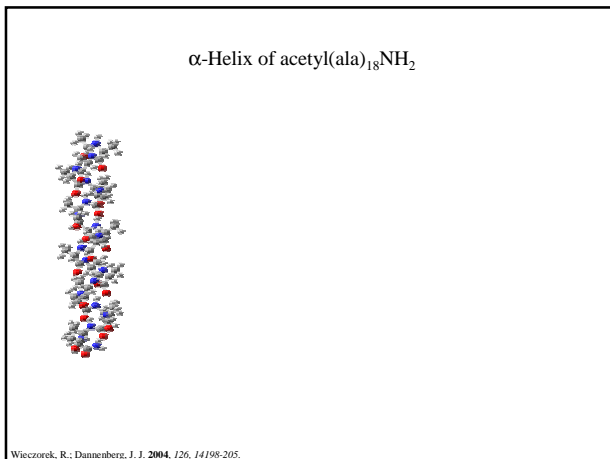
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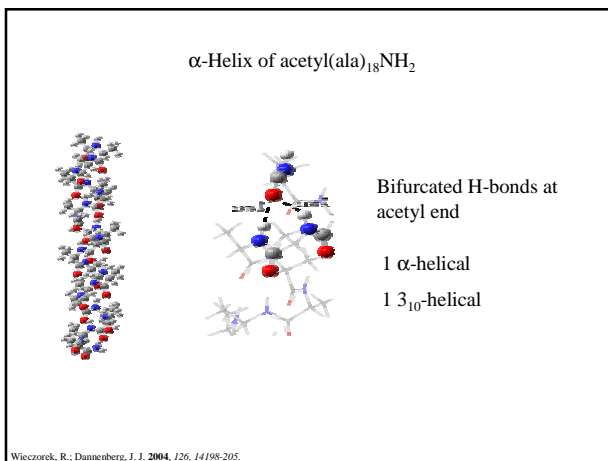
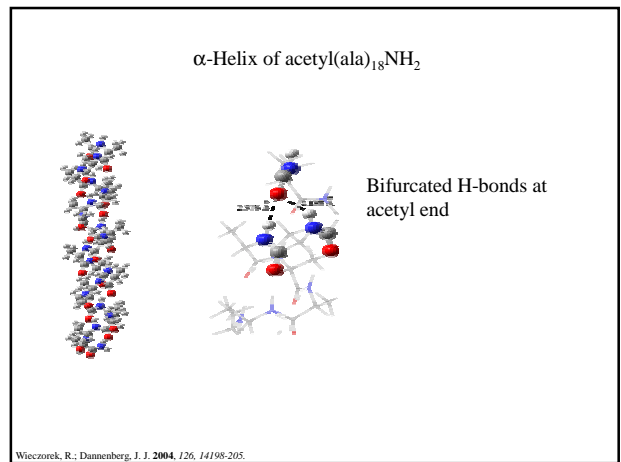
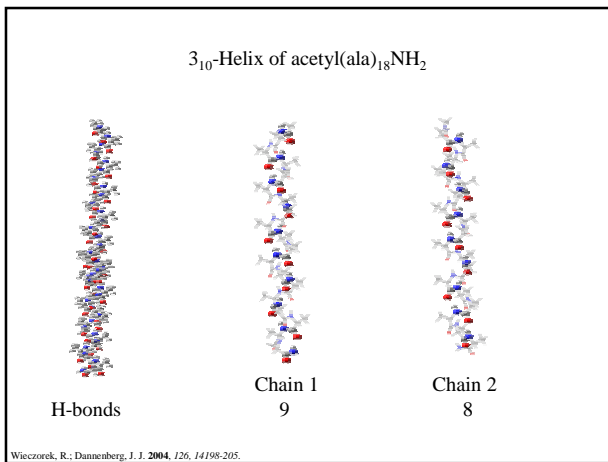
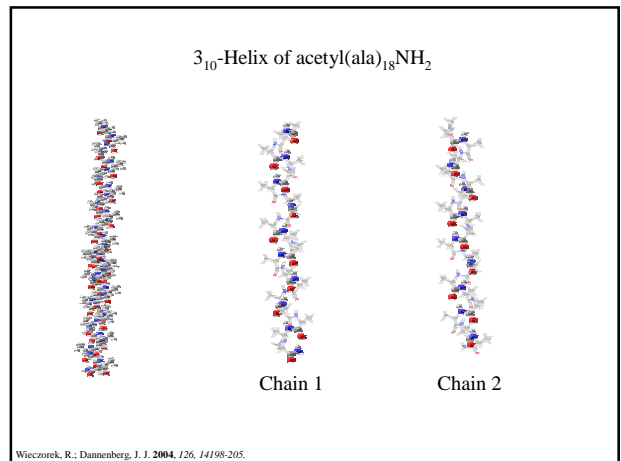
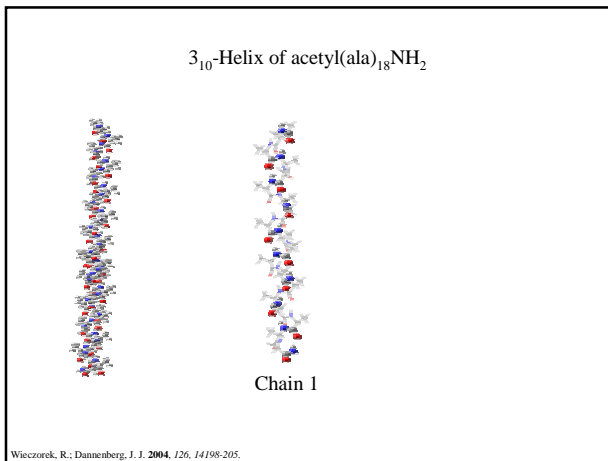
### Comparison of secondary structures of acetyl(ala)<sub>N</sub>NH<sub>2</sub> as a function of N

### β-Strand of acetyl(ala)<sub>18</sub>NH<sub>2</sub>



Wieczorek, R.; Dannenberg, J. J. 2004, 126, 14198-205.



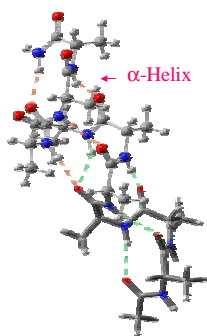


For acetyl(ala)<sub>N</sub>NH<sub>2</sub>:

$\alpha$ -helices are only stable for N=8,10 and 12 or greater

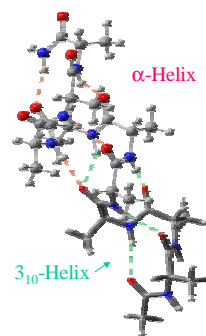
N=6,7,9,11 are mixed helices

Helix of acetyl(ala)<sub>n</sub>NH<sub>2</sub>



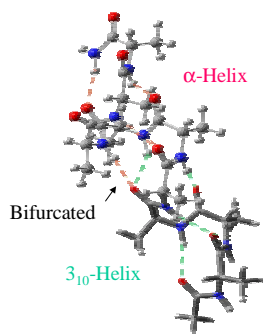
Wieczorek, R.; Dannenberg, J. J. 2004, submitted for publication.

Helix of acetyl(ala)<sub>n</sub>NH<sub>2</sub>



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### Relative energies of capped polyalanines in different secondary structures

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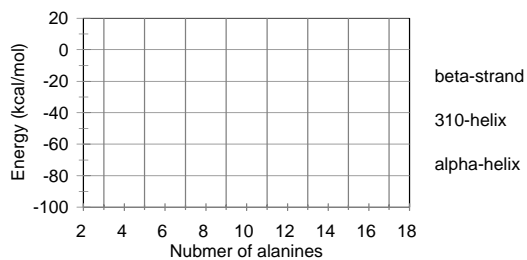
### Relative energies of capped polyalanines in different secondary structures

Acetyl(ala)<sub>N</sub>NH<sub>2</sub>  
N varies from 2 to 18

We calculate the energy of polymerization for each of three secondary structures using the following relationship:

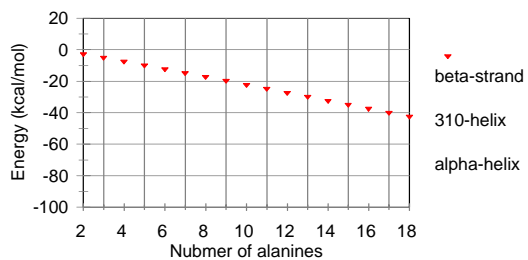
$$E_{\text{polymerization}} = E_{\text{peptide}} - E_{\text{CH}_3\text{COOH}} - E_{\text{NH}_3} - NE_{\text{alanine}} - (N + 1)E_{\text{H}_2\text{O}}$$

### Energies of Reaction



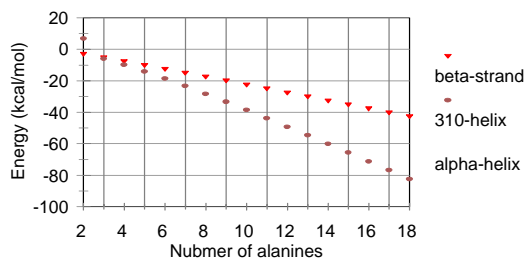
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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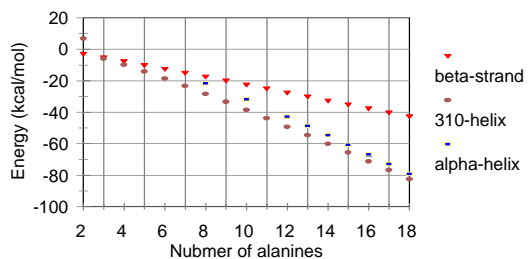
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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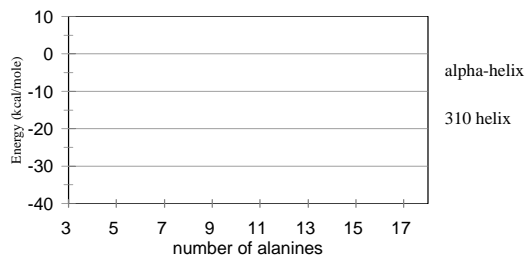
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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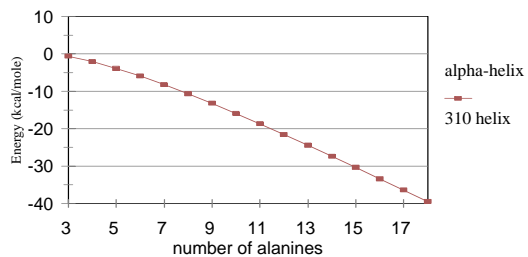
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

### Energy vs beta-strand



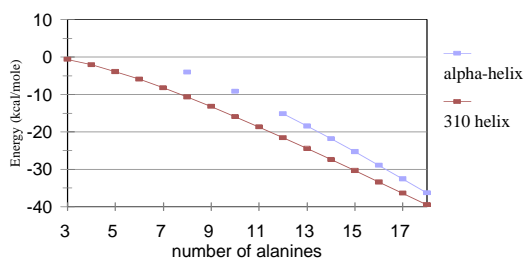
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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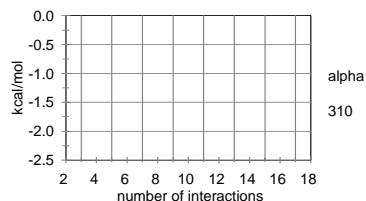
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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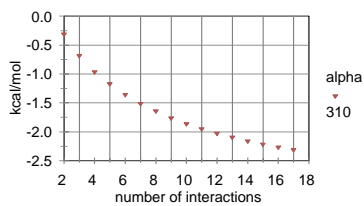
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

### Energy per Peptide Interaction relative to beta-strand



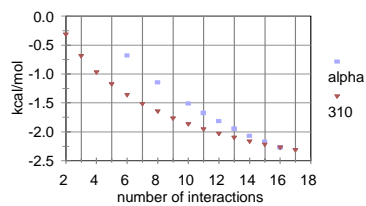
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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### Incremental Stabilities

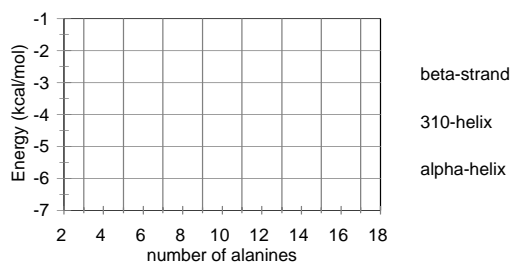
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

### Incremental Stabilities

The difference in the  $E_{\text{polymerization}}$  between  $\text{Ac}(\text{ala})_N\text{NH}_2$  and  $\text{ac}(\text{ala})_{N-1}\text{NH}_2$

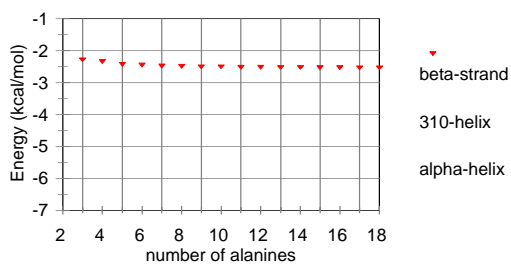
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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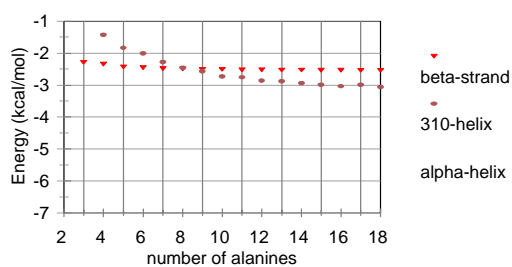
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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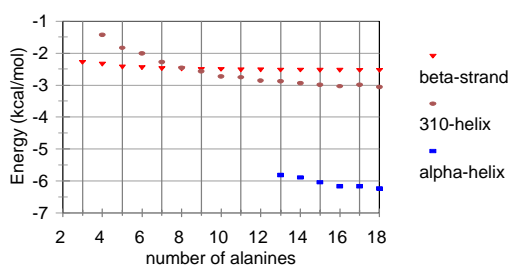
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

### Helical strain per H-bond

Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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Peptide backbone must accommodate the H-bonds

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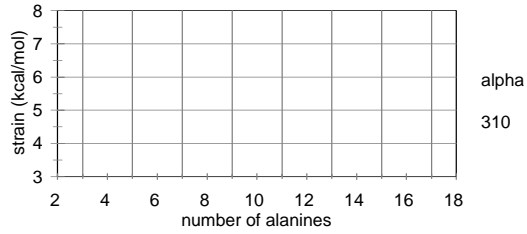
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- 4) We divide by the number of H-bonds in the system

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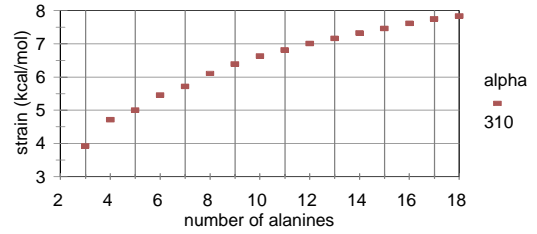


### Helical Strain Per H-Bond



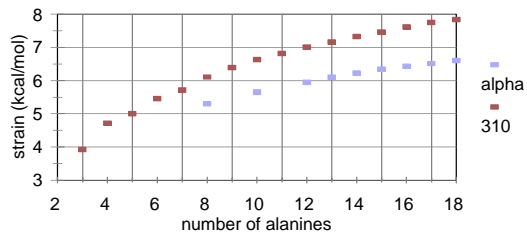
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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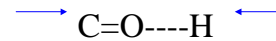
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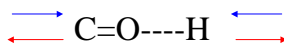


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Stronger H-bond

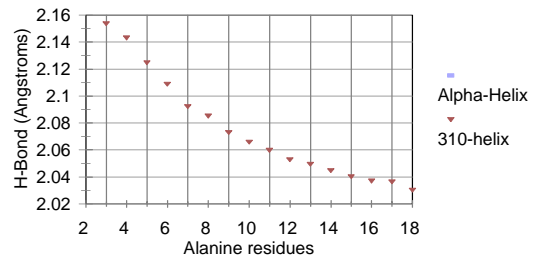


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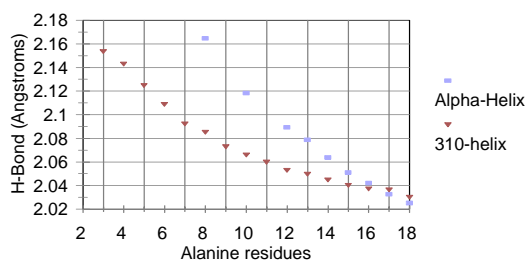
More strain

### Average O...H Distance



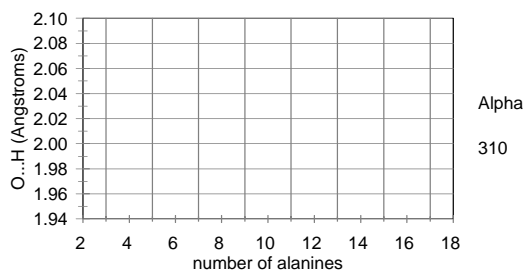
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

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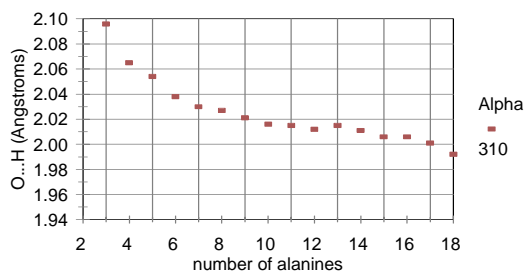
Wiczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205

### Minimum O...H Distances in Helices



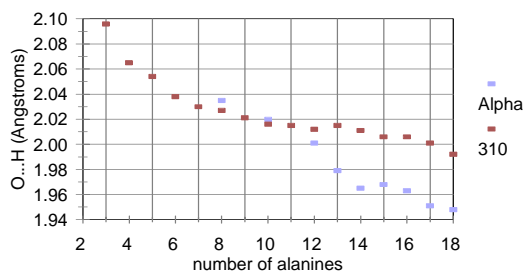
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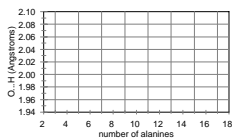
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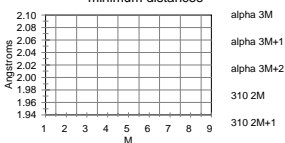


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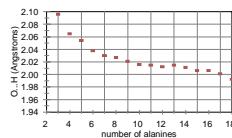


### O...H distances in helix H-bond chains minimum distances

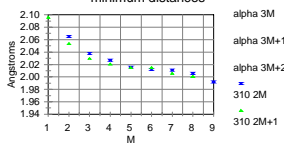


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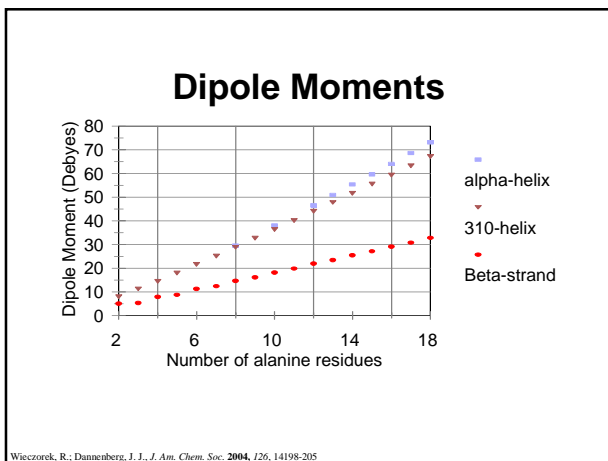
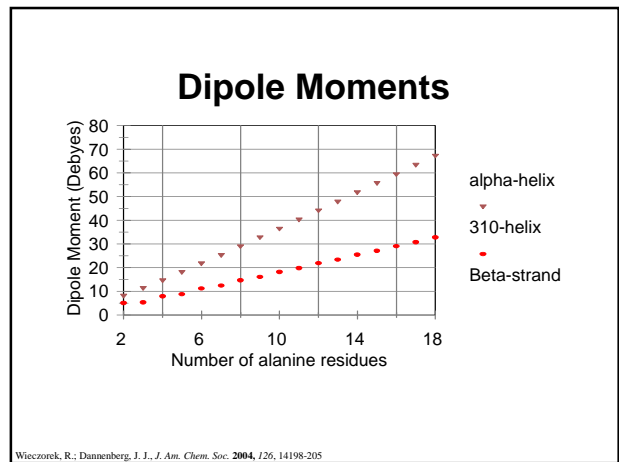
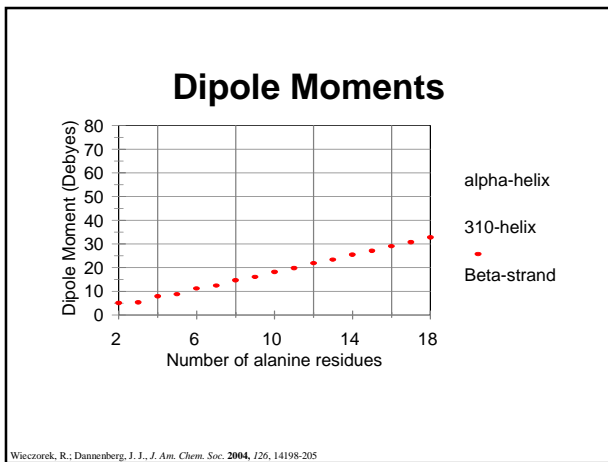
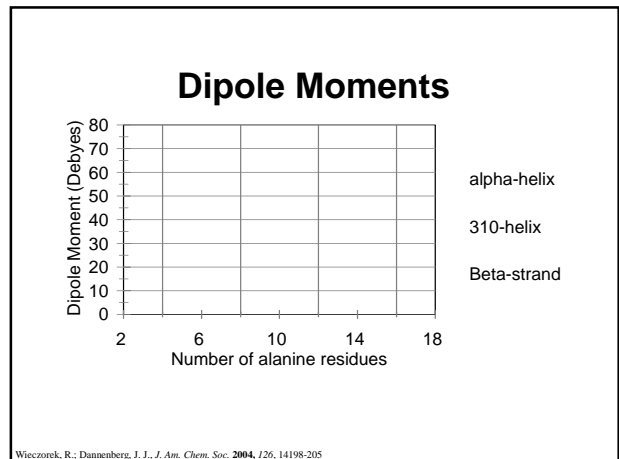
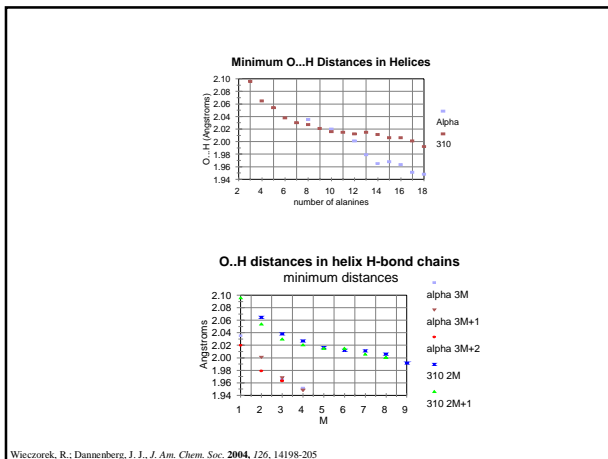
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### O...H distances in helix H-bond chains minimum distances



Wiczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 14198-205



Why are H-bonds in  $\alpha$ -helices more cooperative?

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All of these factors interact with each other

### Protonation of Peptides

Small peptides are zwitter ionic

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Are helical peptides zwitter ions?

## Protonation of Peptides

Small peptides are zwitter ionic

Are helical peptides zwitter ions?

If so, they should protonate most easily on  $\text{NH}_2$

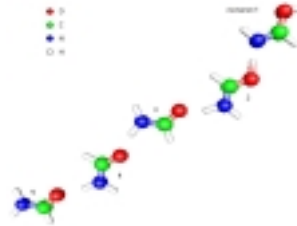
## Protonation of Peptides

Models:

Formamide chains

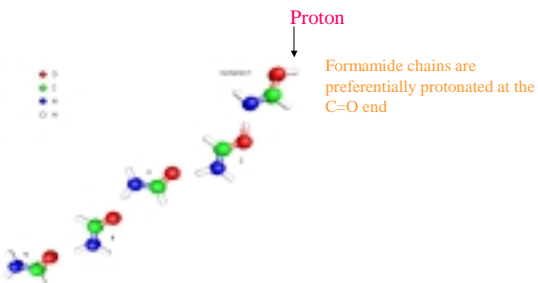
$\alpha$ -helices

## Protonated Formamide Chains



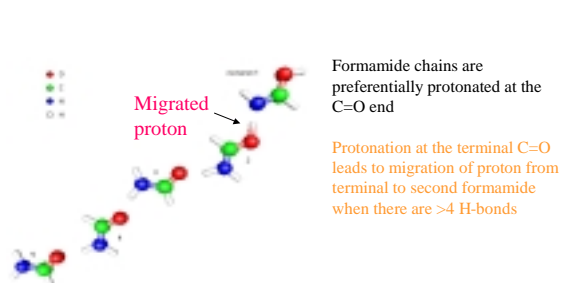
Moisan, S.; Dannenberg, J. J. *J. Phys. Chem. B* **2003**, *107*, 12842

## Protonated Formamide Chains



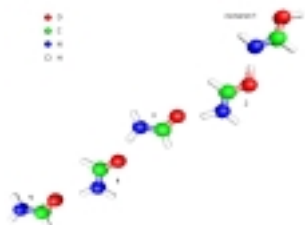
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Moisan, S.; Dannenberg, J. J. *J. Phys. Chem. B* **2003**, *107*, 12842

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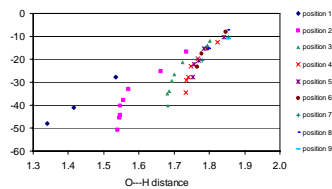
Formamide chains are preferentially protonated at the C=O end

Protonation at the terminal C=O leads to migration of proton from terminal to second formamide when there are >4 H-bonds

Protonation at NH<sub>2</sub> breaks H-bond between protonated and next formamide

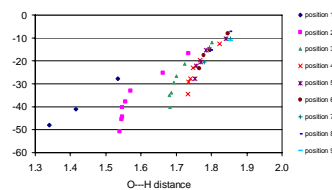
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H-bond enthalpies at 298 K as a function of O...H distance for protonated formamide chains.



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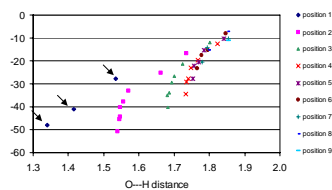
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The relationship between O...H and H-bond strength is no longer linear

Moisan, S.; Dannenberg, J. J. *J. Phys. Chem. B* 2003, 107, 12842

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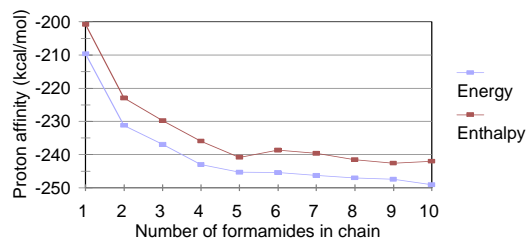


The relationship between O...H and H-bond strength is no longer linear  
The O...H distance for position 1 decreases markedly until the proton migrates

Moisan, S.; Dannenberg, J. J. *J. Phys. Chem. B* 2003, 107, 12842

### Protonated Formamide Chains

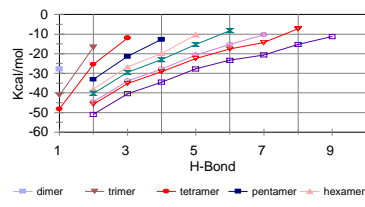
#### Proton Affinities



Moisan, S.; Dannenberg, J. J. *J. Phys. Chem. B* 2003, 107, 12842

### H-Bond Energies in Protonated Formamide Chains

#### Protonated Formamide H-Bond Energies



Proton in first H-bond is transferred to second formamide in aggregates with five or more monomers

Moisan, S.; Dannenberg, J. J. *J. Phys. Chem. B* 2003, 107, 12842

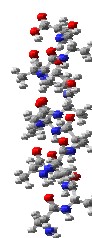
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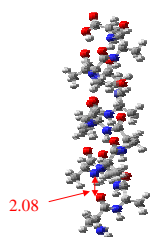
$\alpha$ -helices

Proton affinities of ala<sub>14</sub>



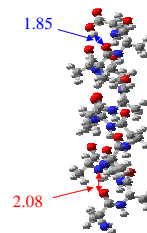
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 12278-9

Proton affinities of ala<sub>14</sub>



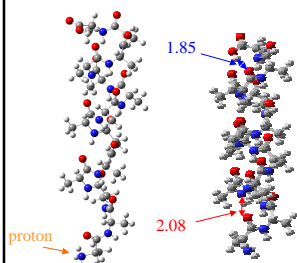
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 12278-9

Proton affinities of ala<sub>14</sub>



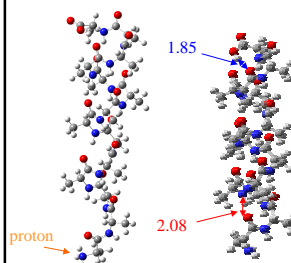
Wieczorek, R.; Dannenberg, J. J., *J. Am. Chem. Soc.* **2004**, *126*, 12278-9

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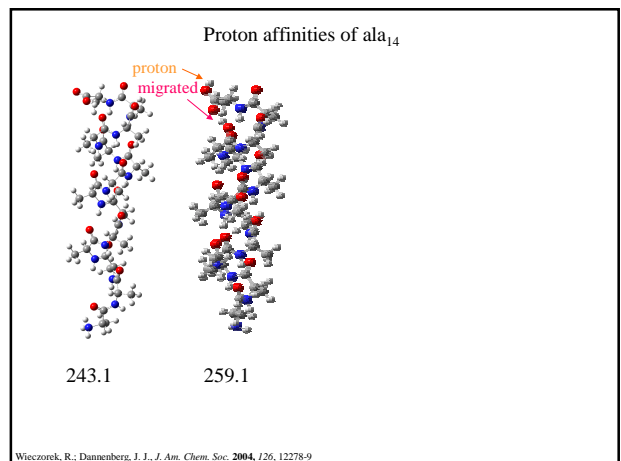
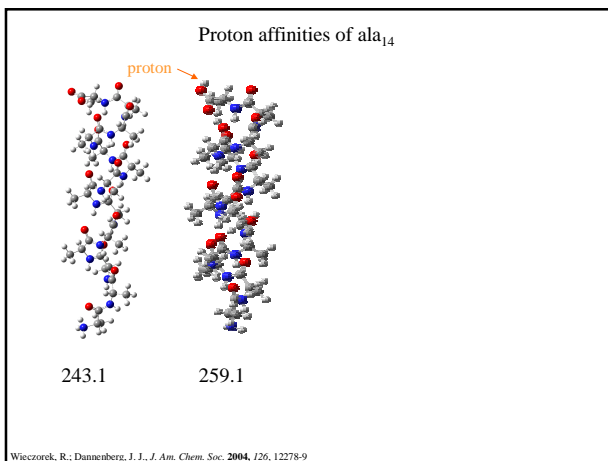
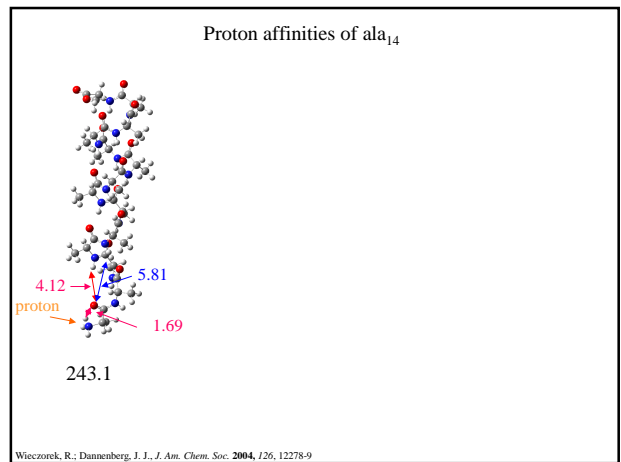
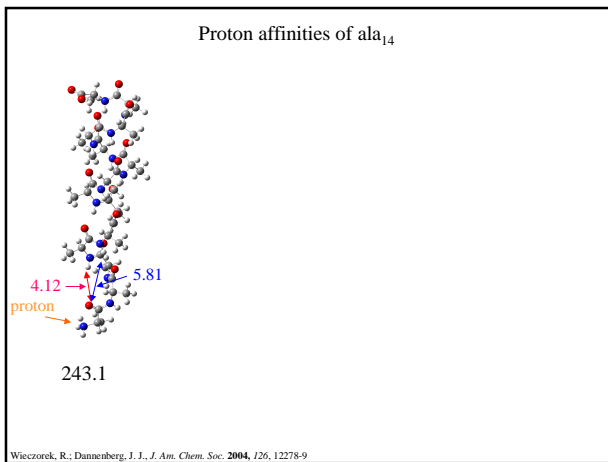
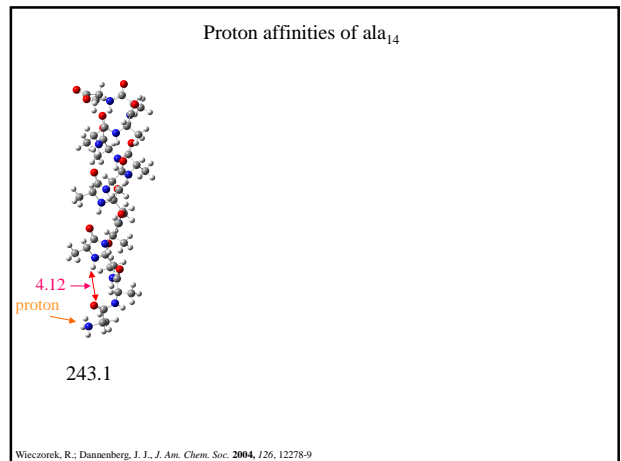
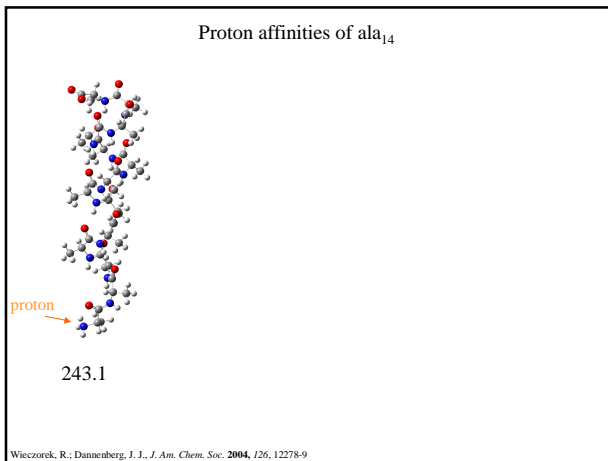


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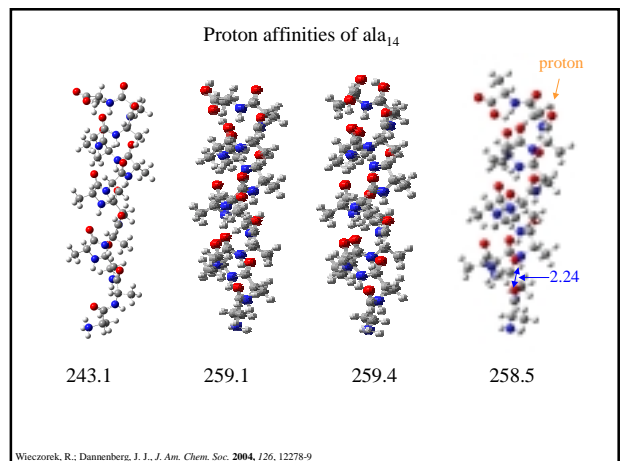
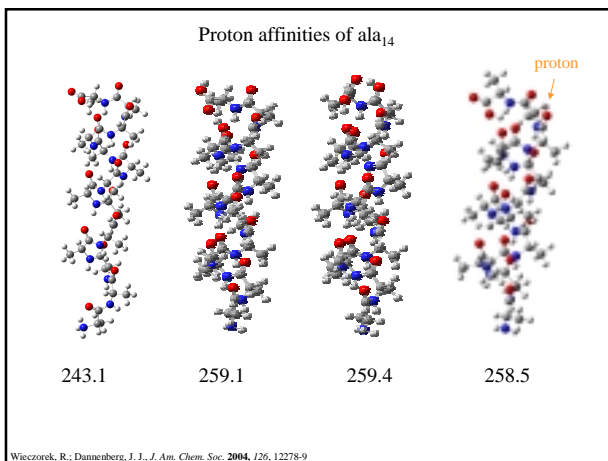
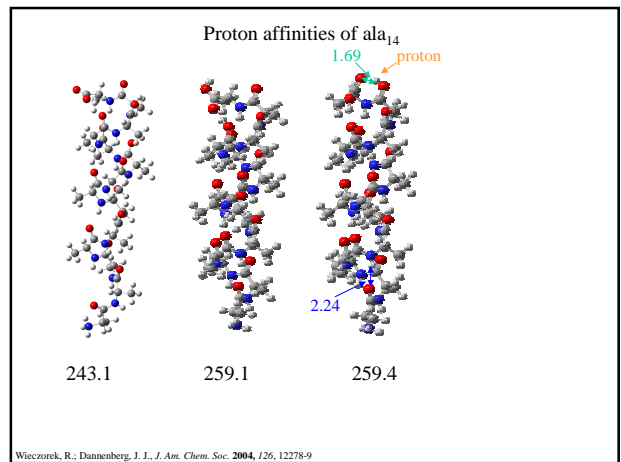
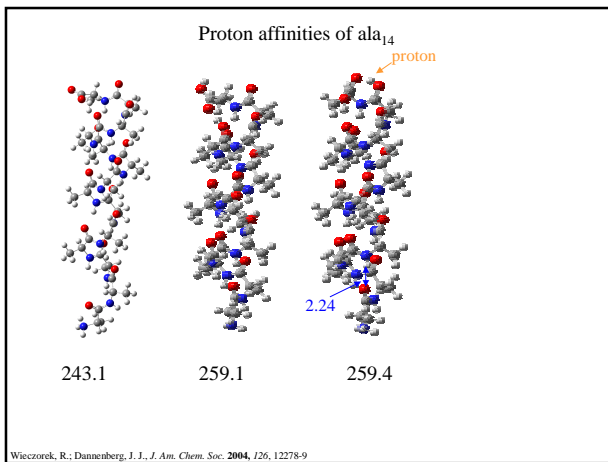
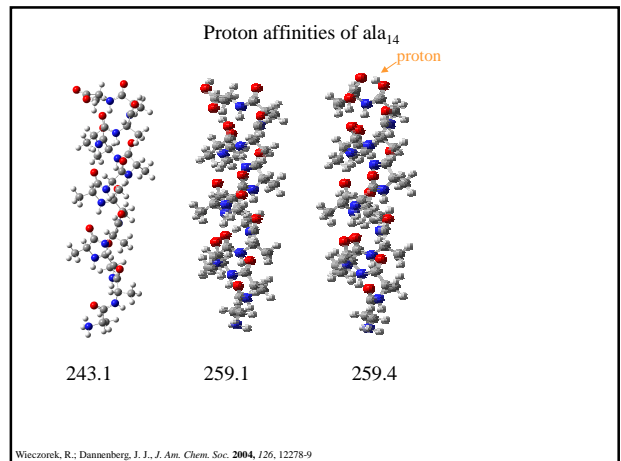
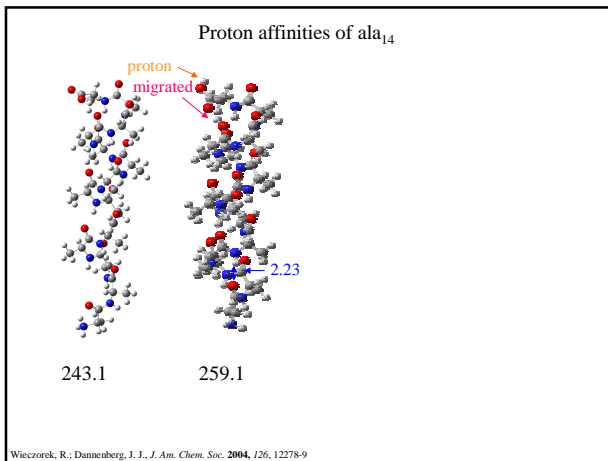
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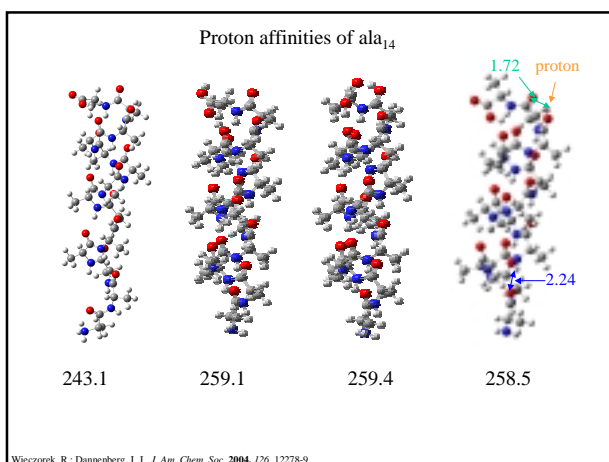


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Comparison of proton affinities of ala<sub>14</sub> and ala<sub>17</sub>  
kcal/mol

Ala's	COOH	1 <sup>st</sup> C=O	2 <sup>nd</sup> C=O	NH <sub>2</sub>
8	259.1	259.3	258.5	243.1
14	272.3	274.0	274.7	212.6
17	276.5	278.0	279.0	202.5

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β-Sheets

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β-strands that are models of two glycines

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β-strands that are models of two glycines, four glycines

## $\beta$ -Sheets

$\beta$ -strands that are models of two glycines, four glycines and two glycines with a  $\text{CH}_2\text{CH}_2$  spacer

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Two and four stranded sheets

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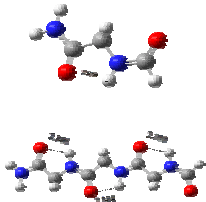
Two and four stranded sheets that maintain a center of symmetry ( $\text{C}_{2\text{H}}$ )

## $\beta$ -Sheets of polyglycines



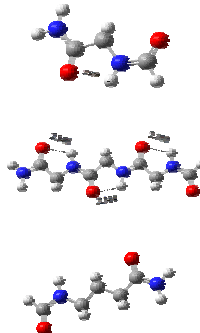
Viswanathan, R.; Asensio, A.; Dannenberg, J. J., *J. Phys. Chem. A* **2004**, *108*, 9205-12

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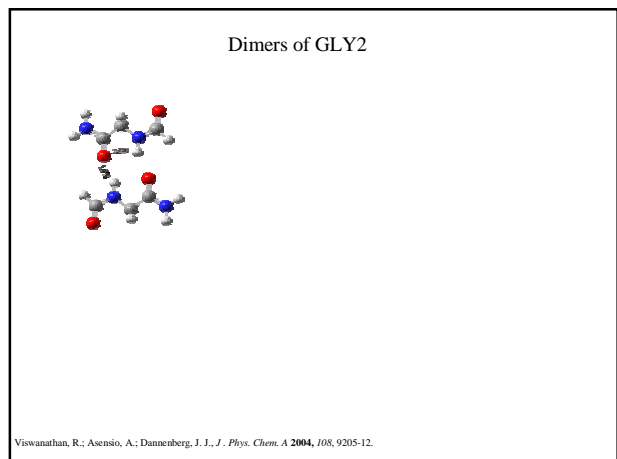
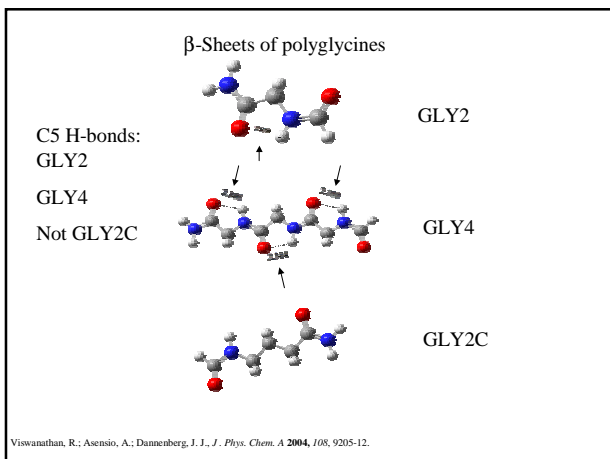
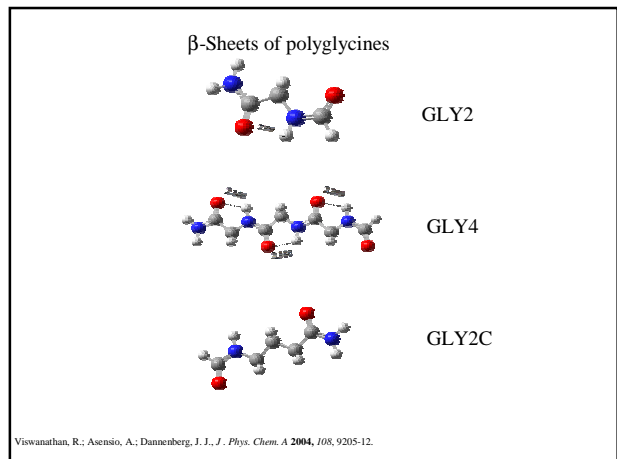
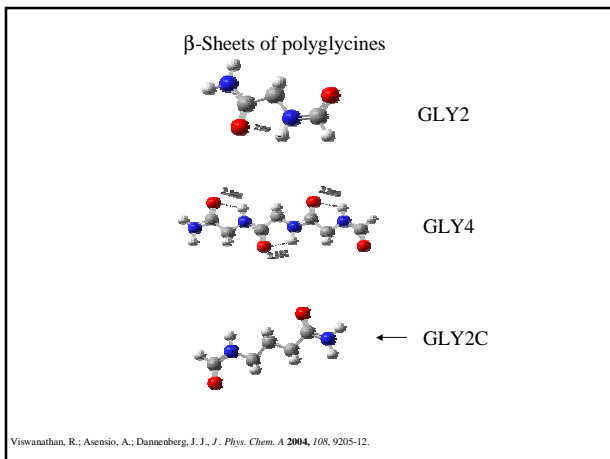
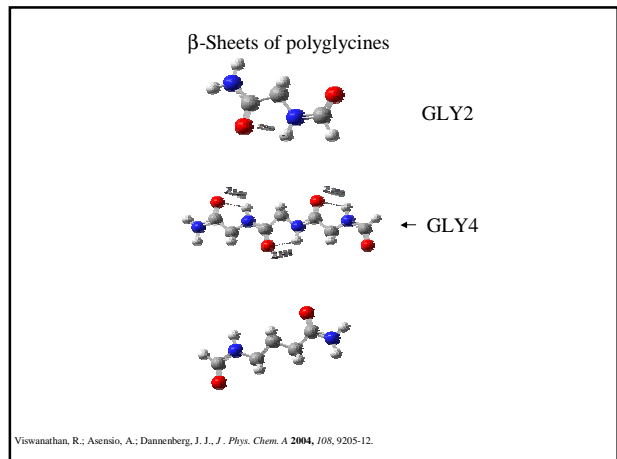
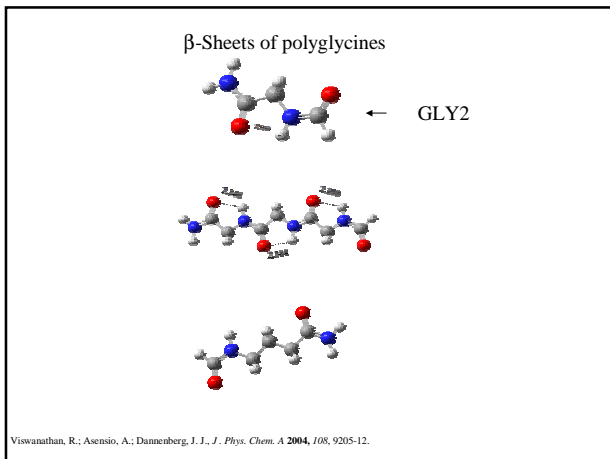


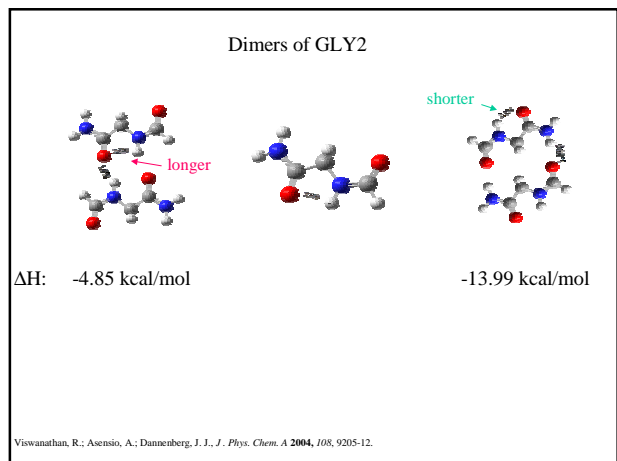
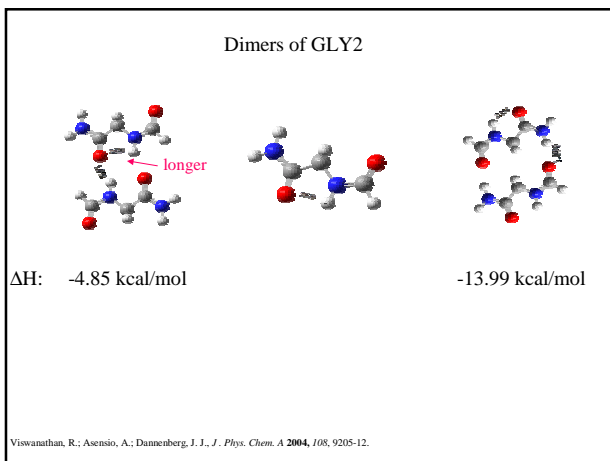
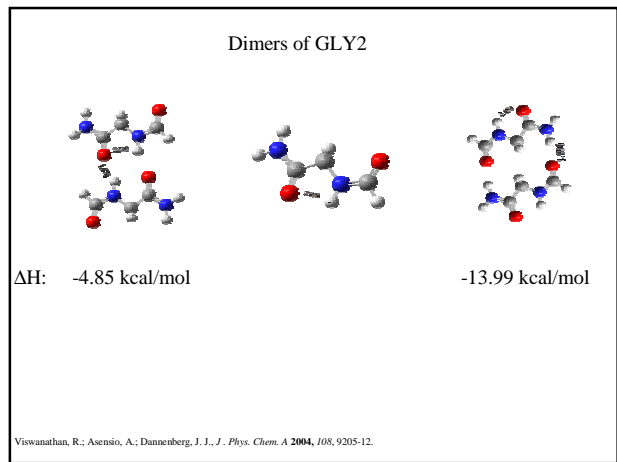
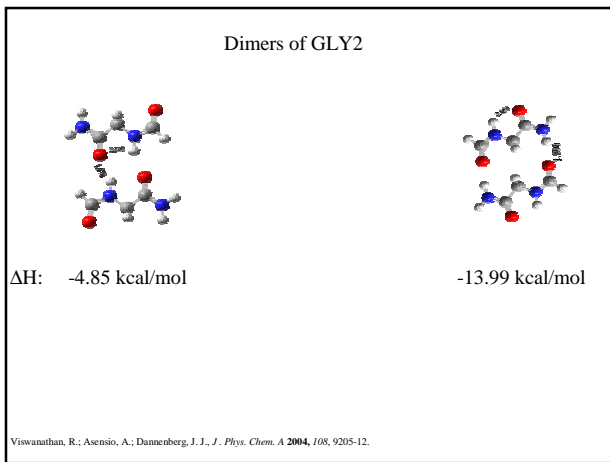
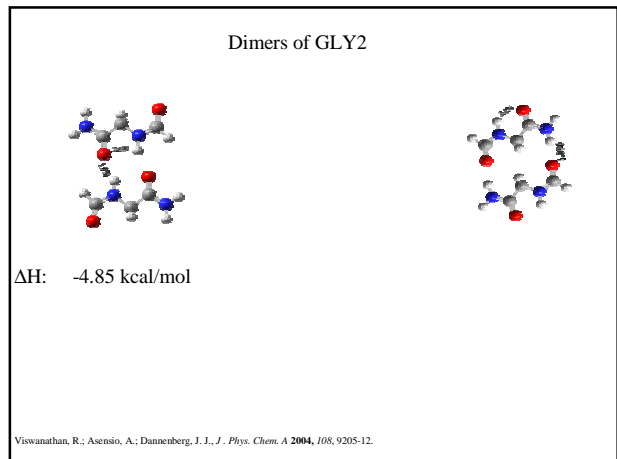
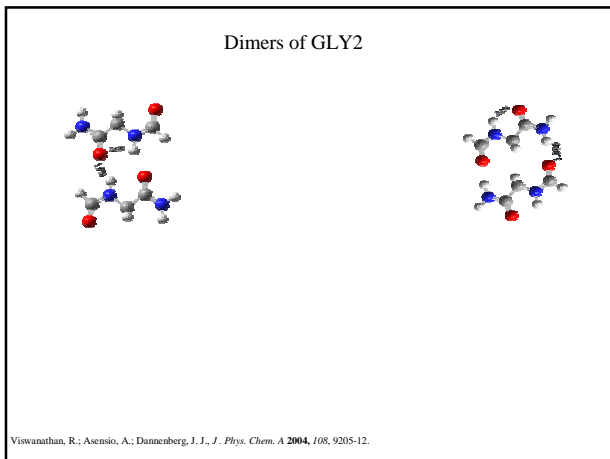
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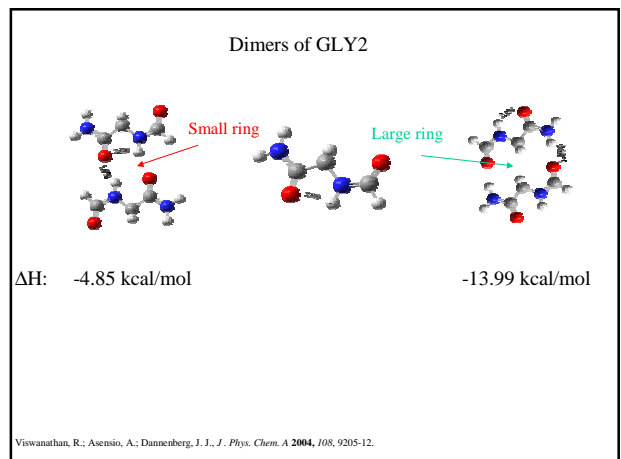
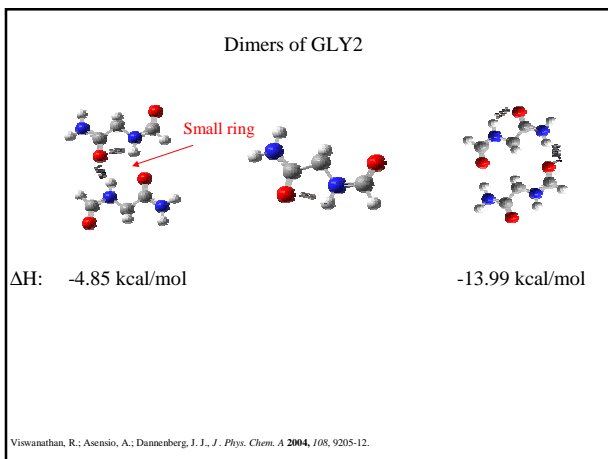
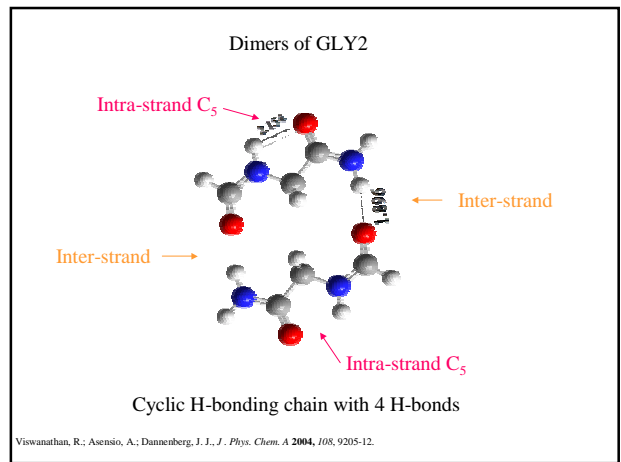
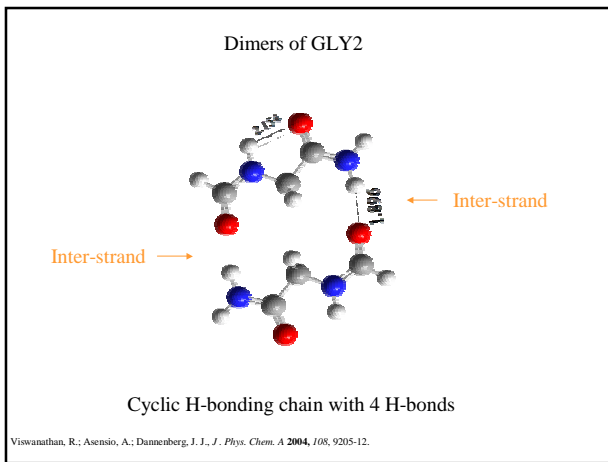
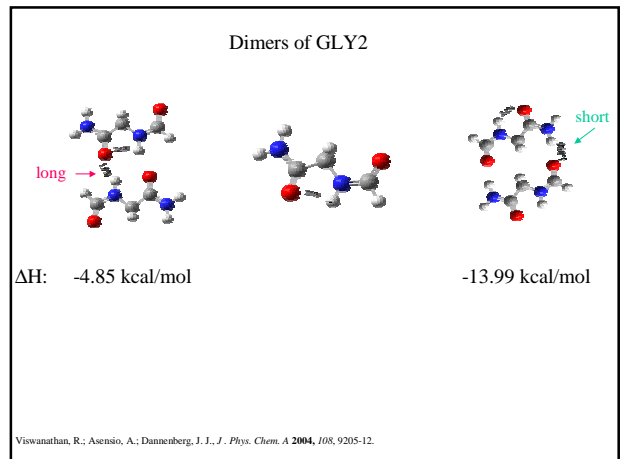
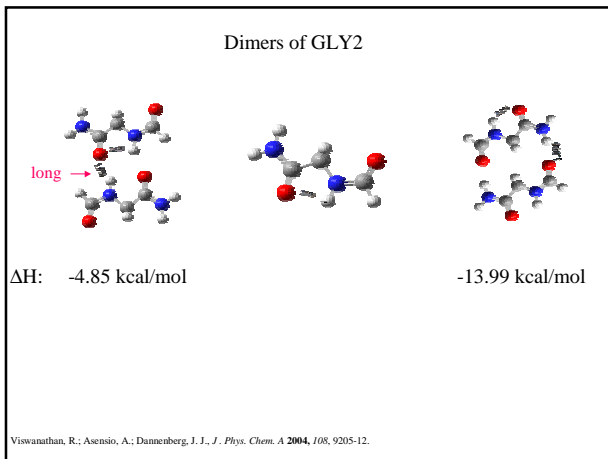
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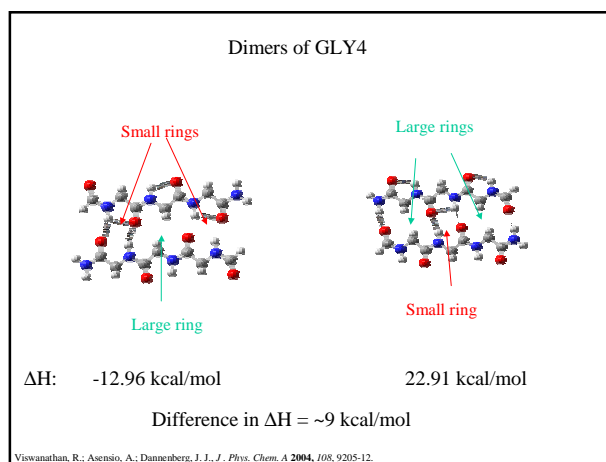
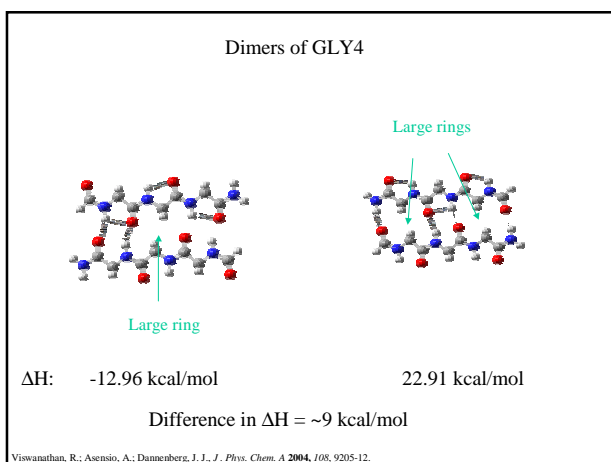
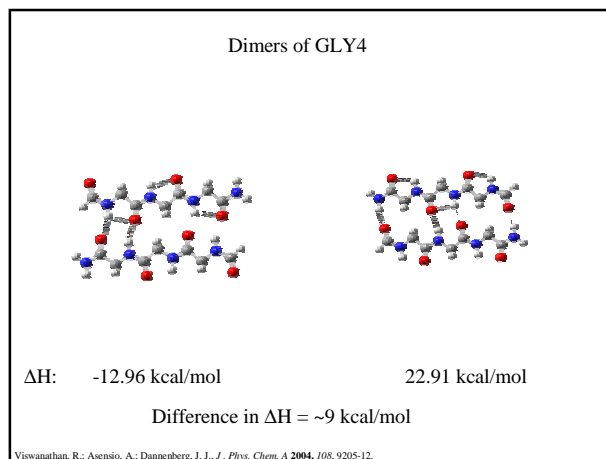
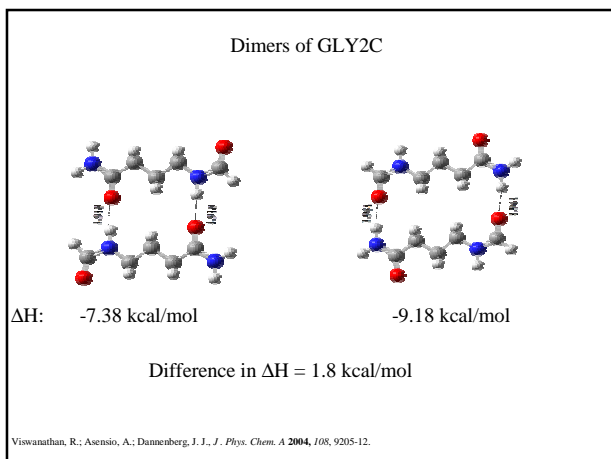
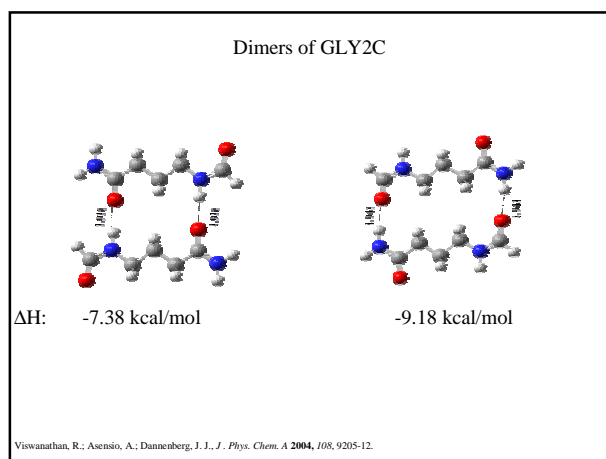
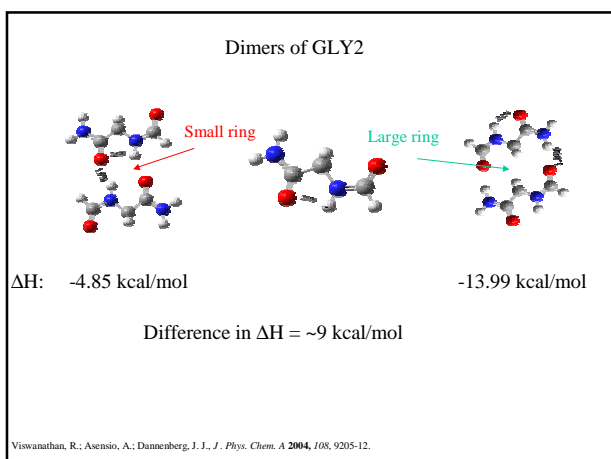


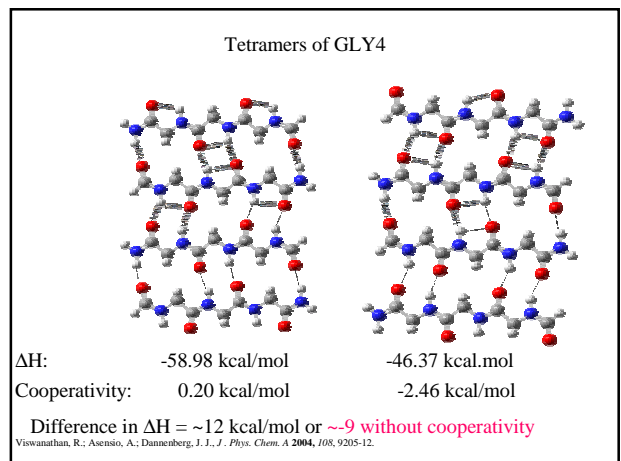
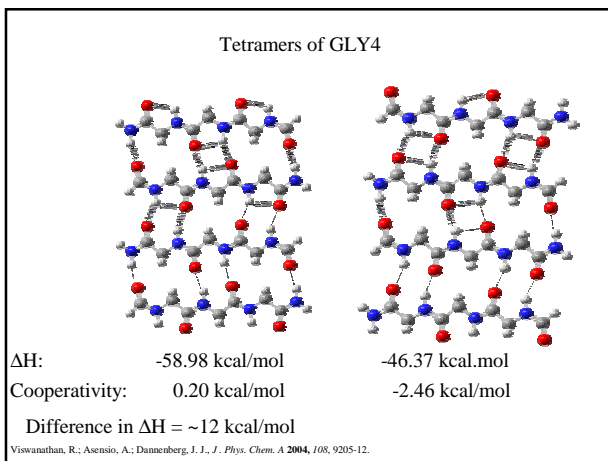
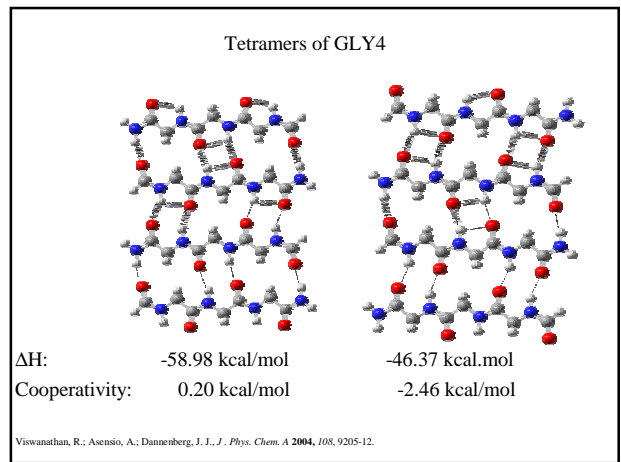
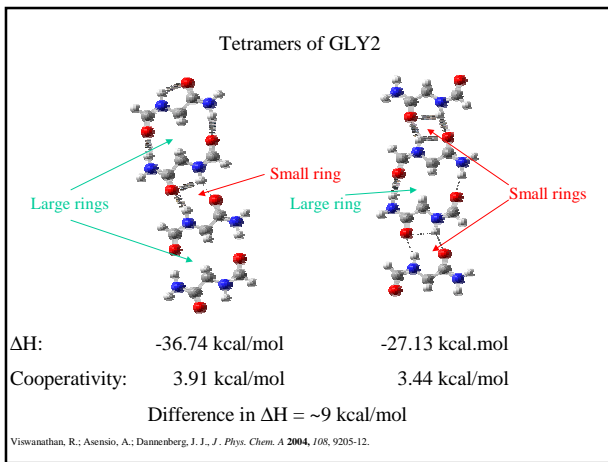
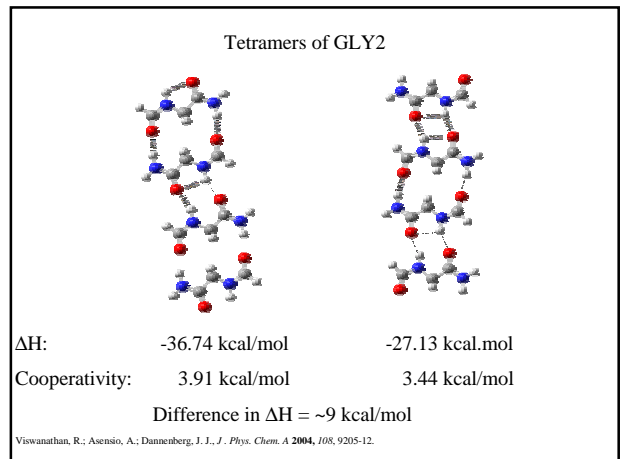
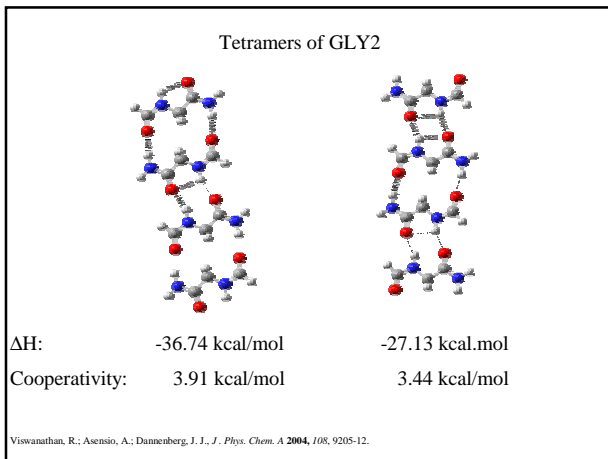
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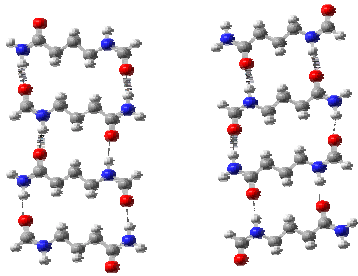








Tetramers of GLY2C



$\Delta H$ :            -32.35 kcal/mol            -31.19 kcal/mol

Cooperativity:    6.61 kcal/mol                7.25 kcal/mol

Viswanathan, R.; Asensio, A.; Dannenberg, J.J., *J. Phys. Chem. A* 2004, 108, 9205-12.

Little or no Cooperativity apparent in  $\beta$ -sheets

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Implications for amyloid diseases:

Which sequences will allow H-bond cooperativity?

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Understanding H-bond cooperativity is essential for predicting protein folding

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Robert Wieczorek  
Pedro Salvador  
Raji Viswanathan  
Amparo Asensio  
Sandy Moisan  
Artem Masunov  
Midas Tsai



Funding  
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